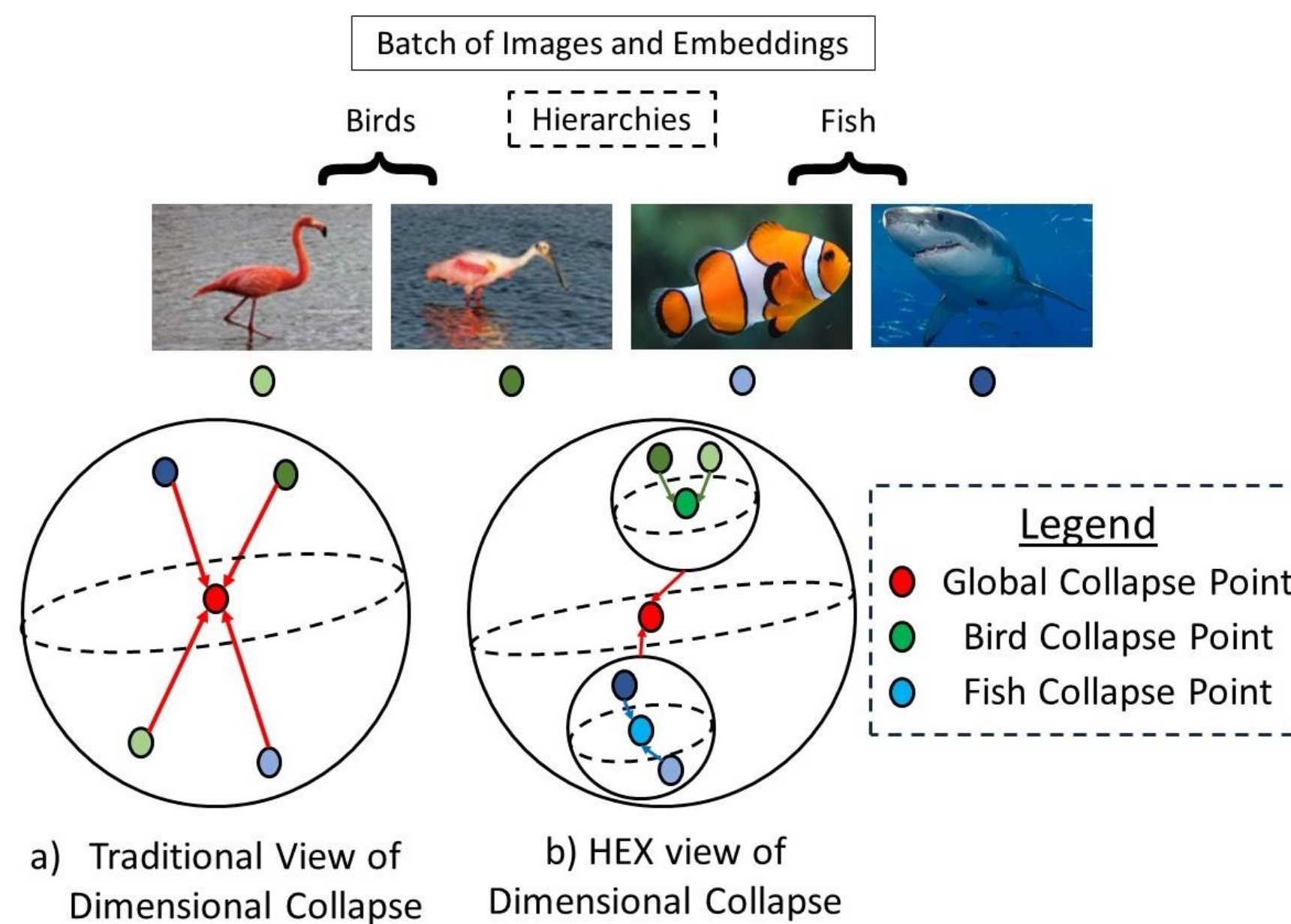
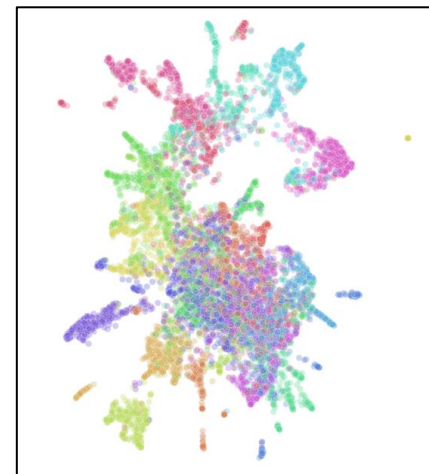


Motivation

50 Epochs of Training



450 Epochs of Training

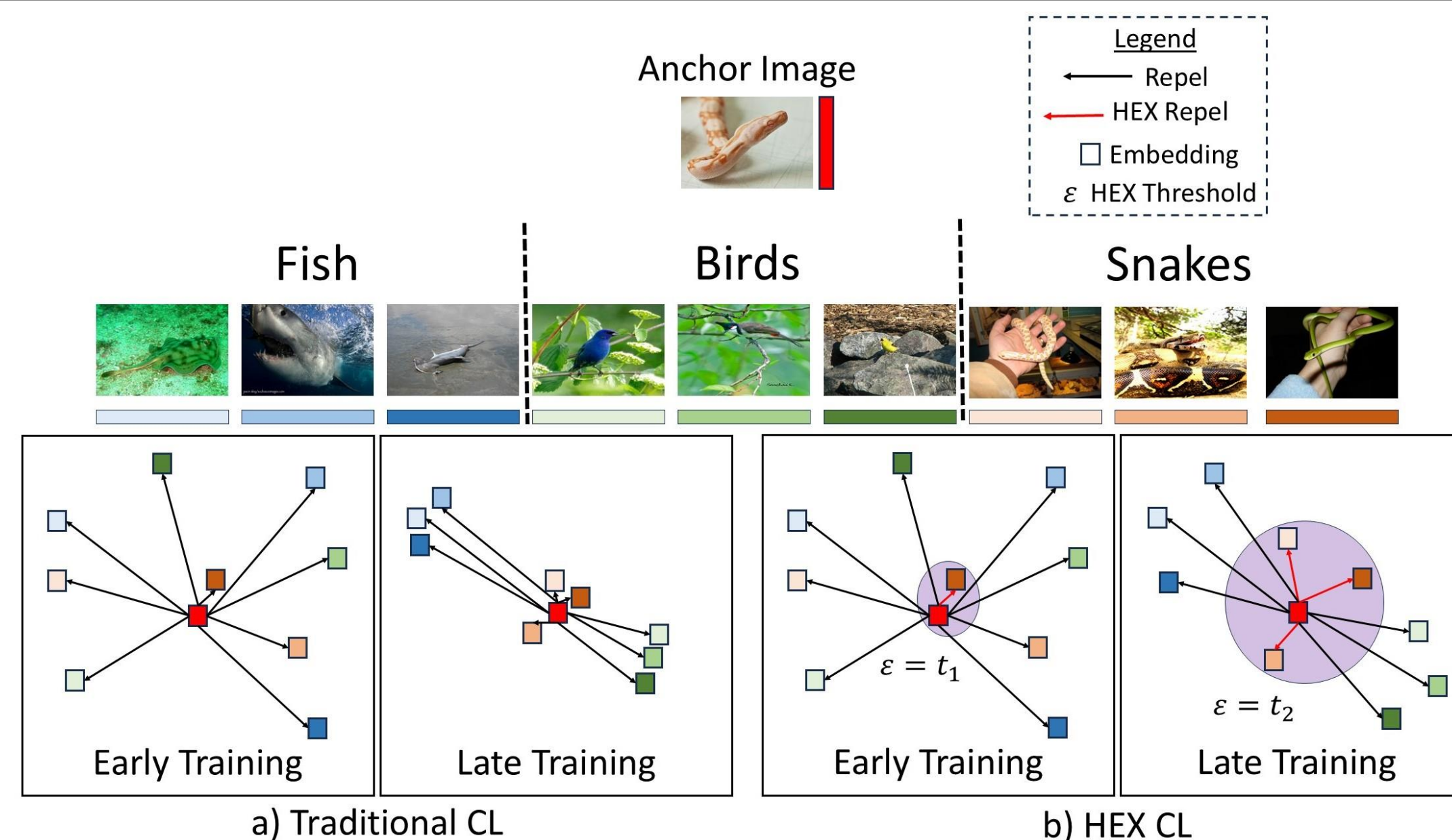


Observations

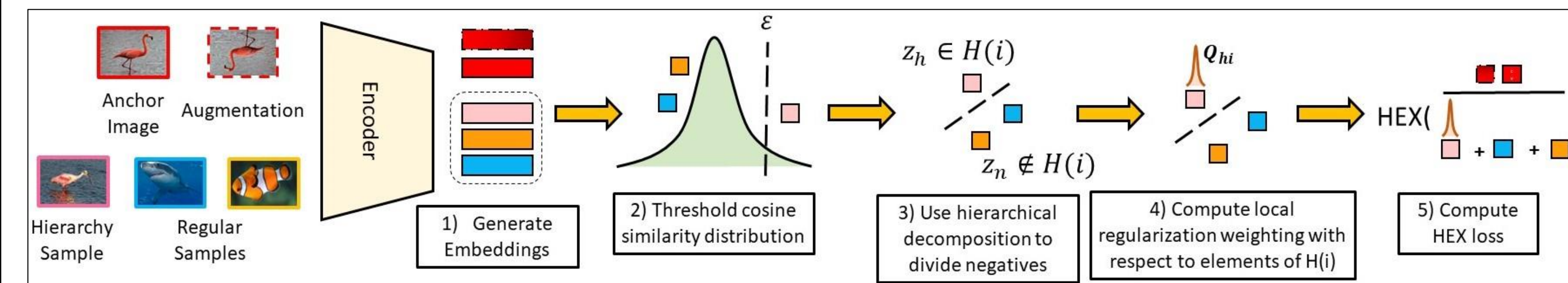
1. SSL algorithms are optimized to prevent **global dimensional** collapse.
2. Classes of **same hierarchy** can share features which collapses locally.
3. Hierarchies **emerge naturally** during training of SSL algorithm.

HEX Intuition

Local hierarchies emerge. Can we exploit this behavior?



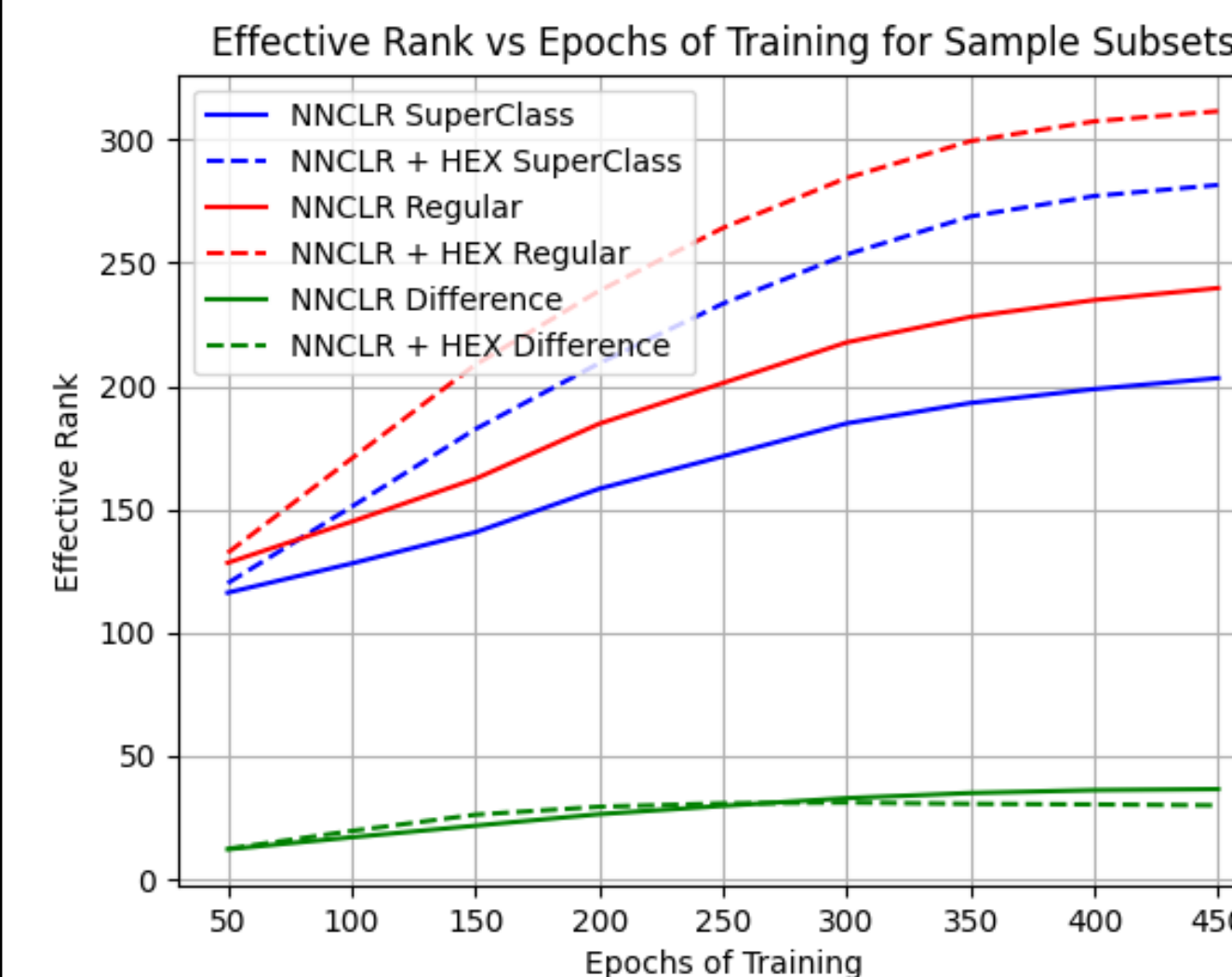
Methodology



$$L_{HEX} = - \sum_{i \in I} \log \left(\frac{\exp \left(z_i \cdot \frac{z_{j(i)}}{\tau} \right)}{Q_{hi} \left(\sum_{h \in H(i)} \exp \left(z_i \cdot \frac{z_h}{\tau} \right) \right) + \sum_{n \notin T(i)} \exp \left(z_i \cdot \frac{z_n}{\tau} \right)} \right)$$

z_i = embedding of anchor image
 $i \in I$ = anchor image
 $z_{j(i)}$ = embedding of augmentation
 z_h = embedding of hierarchy negatives
 Q_{hi} = weighting function
 z_a = embedding of negatives
 z_n = embedding of regular negatives
 $H(i)$ = Set of Hierarchy Negatives
 τ = Temperature

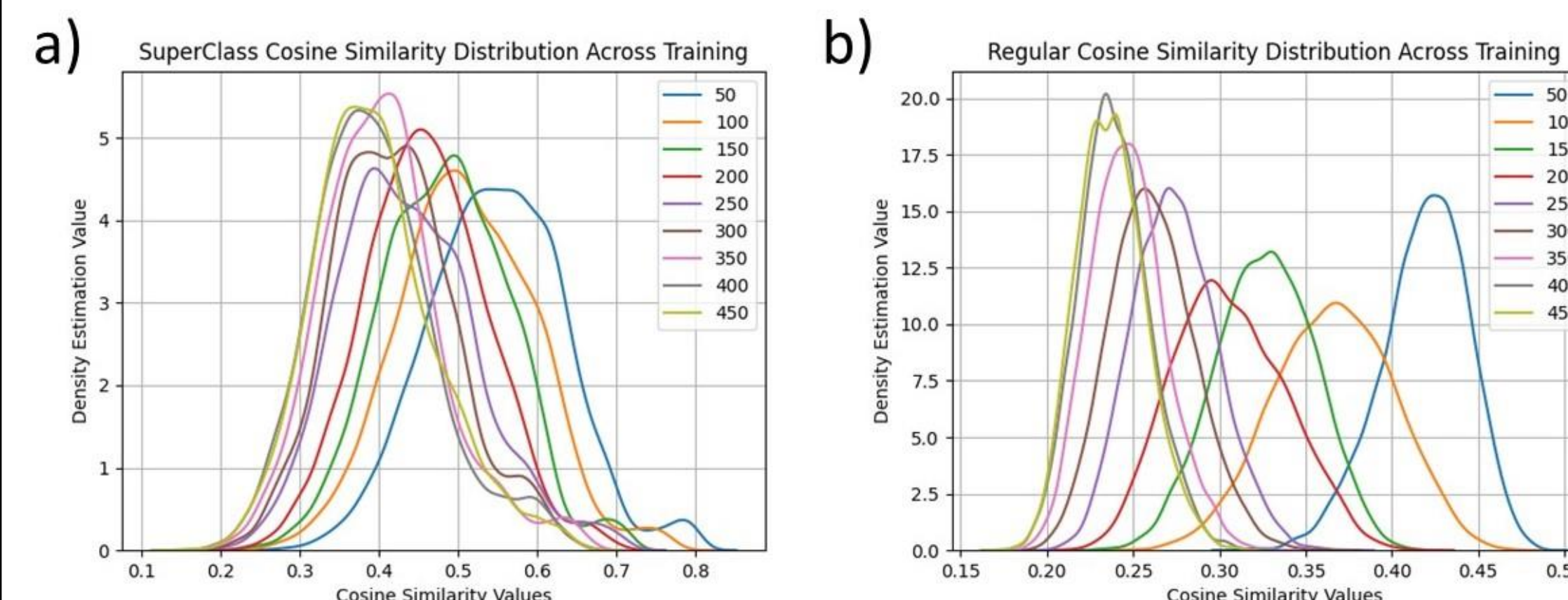
Analysis of Hierarchical Representations



Members of same hierarchy have **greater local collapse**.

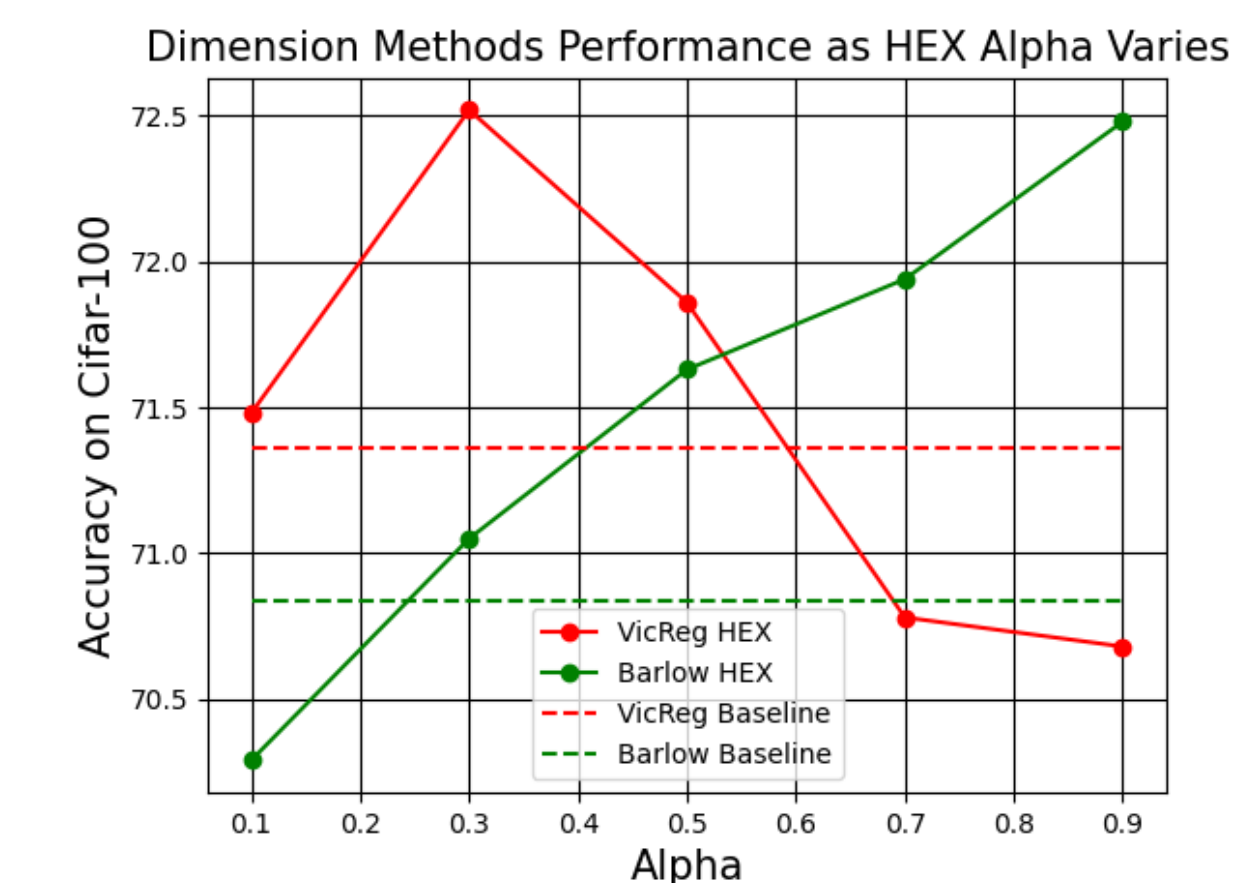
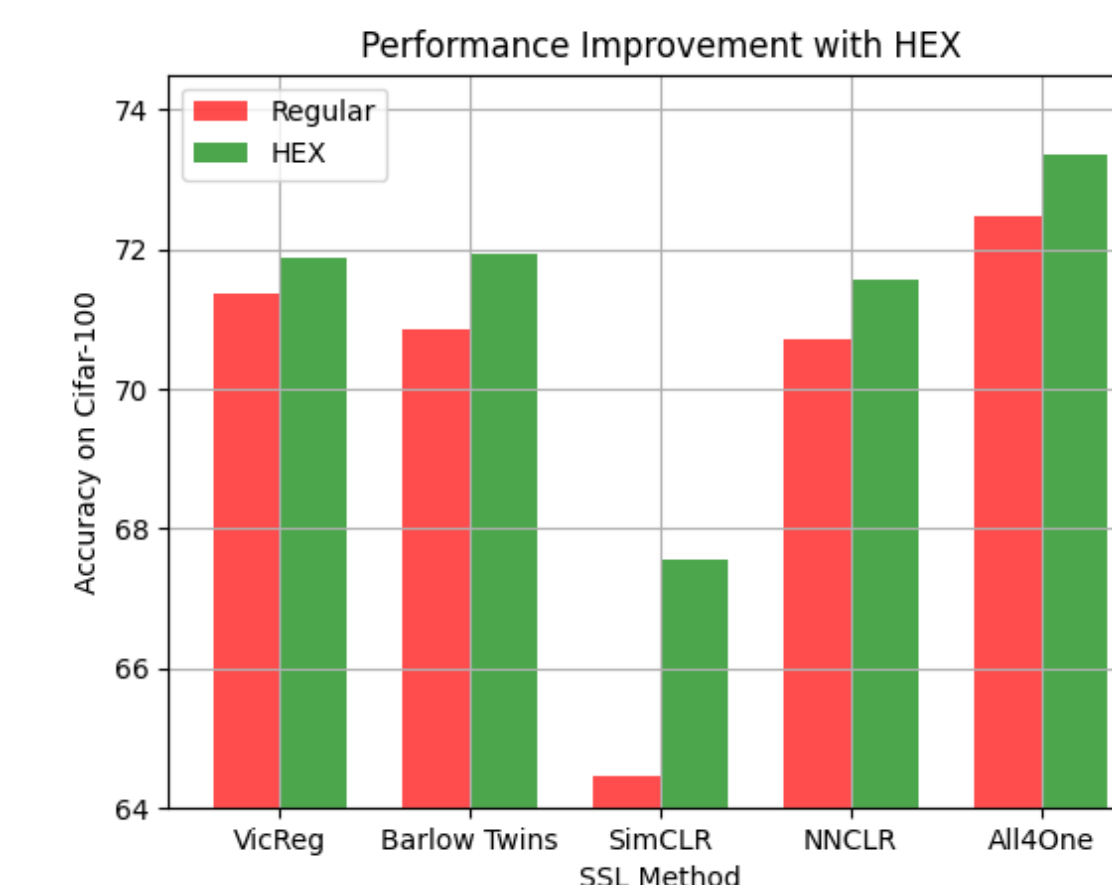
Cosine similarity distribution varies for superclass and regular samples at different epochs.

Can separate hierarchical and regular samples.

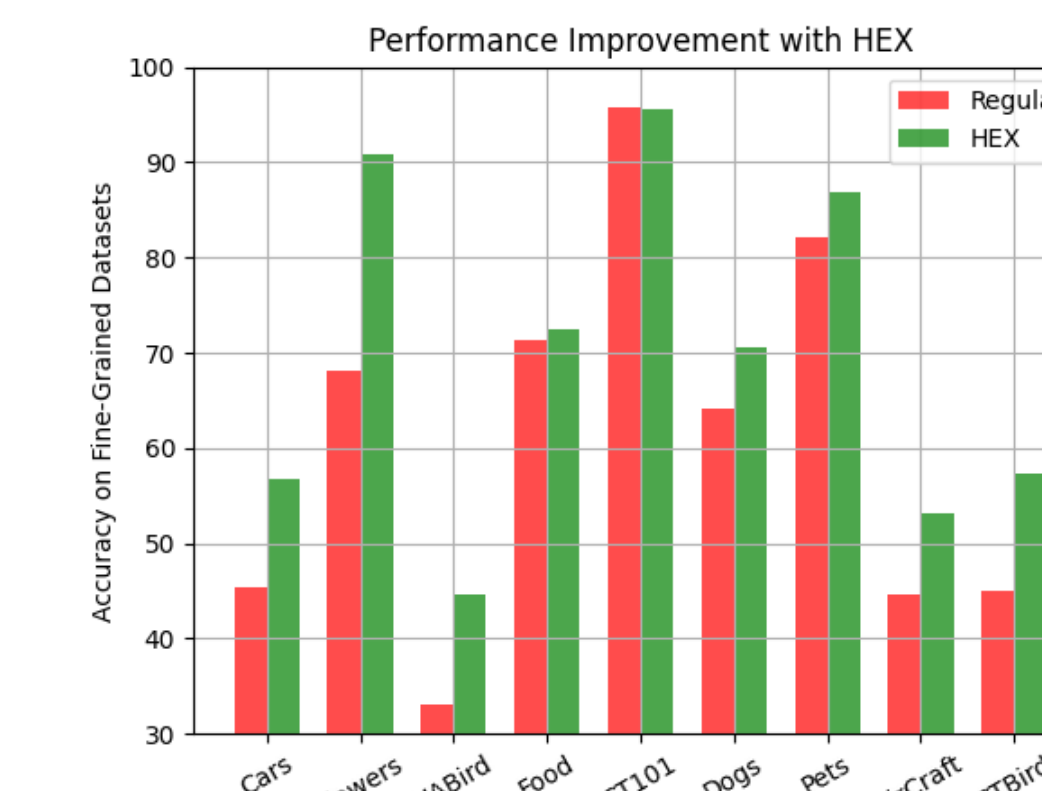


Results

HEX can be applied to both Sample Contrastive and Dimension Contrastive Strategies



Performance improvement consistent across datasets



Method	ImageNet	ImageNet Semi-Supervised (1%)
SimCLR	57.74%	29.61%
SimCLR + HEX	59.03%	33.72%
NNCLR	62.47%	39.94%
NNCLR + HEX	65.96%	46.00%

Conclusion

- We propose a self-supervised methodology based on cosine similarity distributions to **identify the existence of local hierarchical groupings of images** within the representation space.
- We **introduce a local hierarchical regularization into the training process** for both sample and dimension contrastive strategies.
- We introduce an ε **threshold term** during the training process that can be tuned adaptively or manually to reflect the **growing hierarchical organization** of the representation space.